

Confinement symmetry: implications for hadron spectroscopy and high temperatures.

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What is the origin of hadron mass?

Is it possible to separate confinement and chiral symmetry breaking physics?

What physics is responsible for confinement and for chiral symmetry breaking?

Banks-Casher:

$$\langle \bar{q}q \rangle = -\pi\rho(0).$$

What we do:

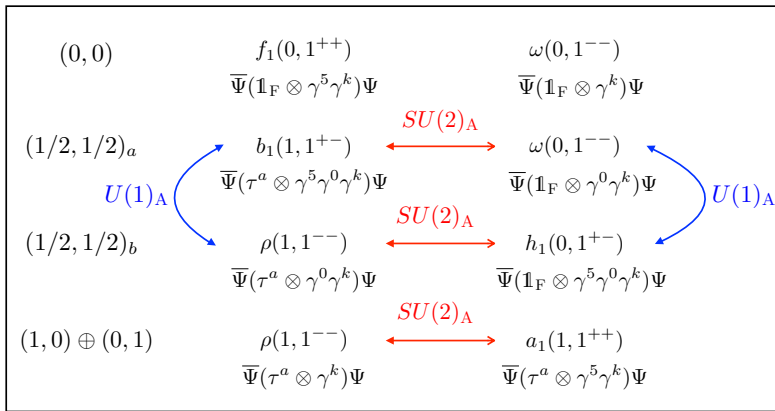
$$S = S_{Full} - \sum_{i=1}^k \frac{1}{\lambda_i} |\lambda_i\rangle\langle\lambda_i|.$$

We use JLQCD $N_f = 2$ overlap gauge configurations.



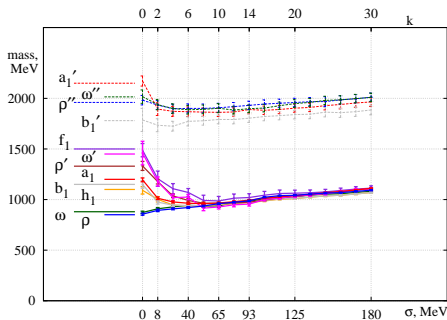
$SU(2)_L \times SU(2)_R$ and $U(1)_A$ partners

What one expects for $J = 1$ mesons:



M.Denissenya, L.Ya.G., C.B.Lang, PRD 89(2014)077502; 91(2015)034505

$$J = 1$$



We clearly see a larger degeneracy than the $SU(2)_L \times SU(2)_R \times U(1)_A$ symmetry of the QCD Lagrangian. What does it mean !?



L.Ya.G., EPJA 51(2015)27

(i) **(0,0):**

$$|(0,0); \pm; J\rangle = \frac{1}{\sqrt{2}} |\bar{R}R \pm \bar{L}L\rangle_J.$$

(ii) **$(1/2, 1/2)_a$ and $(1/2, 1/2)_b$:**

$$|(1/2, 1/2)_a; +; I=0; J\rangle = \frac{1}{\sqrt{2}} |\bar{R}L + \bar{L}R\rangle_J,$$

$$|(1/2, 1/2)_a; -; I=1; J\rangle = \frac{1}{\sqrt{2}} |\bar{R}\tau L - \bar{L}\tau R\rangle_J,$$

$$|(1/2, 1/2)_b; -; I=0; J\rangle = \frac{1}{\sqrt{2}} |\bar{R}L - \bar{L}R\rangle_J,$$

$$|(1/2, 1/2)_b; +; I=1; J\rangle = \frac{1}{\sqrt{2}} |\bar{R}\tau L + \bar{L}\tau R\rangle_J.$$

(iii) **$(0,1) \oplus (1,0)$:**

$$|(0,1) + (1,0); \pm; J\rangle = \frac{1}{\sqrt{2}} |\bar{R}\tau R \pm \bar{L}\tau L\rangle_J,$$



L.Ya.G., EPJA 51(2015)27

Consider rotations in an imaginary 3-dim space of doublets constructed from the Weyl spinors

$$U = \begin{pmatrix} u_L \\ u_R \end{pmatrix} \quad D = \begin{pmatrix} d_L \\ d_R \end{pmatrix}$$

$$U \rightarrow U' = e^{i\frac{\boldsymbol{\varepsilon} \cdot \boldsymbol{\sigma}}{2}} U, \quad D \rightarrow D' = e^{i\frac{\boldsymbol{\varepsilon} \cdot \boldsymbol{\sigma}}{2}} D,$$

where $\boldsymbol{\sigma}$ are the standard Pauli matrices: $[\sigma^i, \sigma^j] = 2i\epsilon^{ijk} \sigma^k$.

We refer to this imaginary three-dimensional space as the **chiral spin** space and denote this symmetry group as $SU(2)_{CS}$

A group that contains at the same time $SU(2)_L \times SU(2)_R$ and $SU(2)_{CS}$ is $SU(4)$ with the fundamental vector

$$\Psi = \begin{pmatrix} u_L \\ u_R \\ d_L \\ d_R \end{pmatrix}$$



L.Ya.G., M. Pak, PRD 92(2015)016001

Instead of the states constructed with Weyl spinors we can consider the left- and right-handed Dirac bispinors and bilinear operators. Then the $SU(2)_{CS}$ chiralspin rotations are generated through

$$\Sigma = \{\gamma^l, -i\gamma^5\gamma^l, \gamma^5\}, \quad l = 1, 2, 3, 4 \quad [\Sigma^i, \Sigma^j] = 2i\epsilon^{ijk} \Sigma^k.$$

The $SU(4)$ group contains at the same time $SU(2)_L \times SU(2)_R$ and $SU(2)_{CS} \supset U(1)_A$ with the fundamental vector

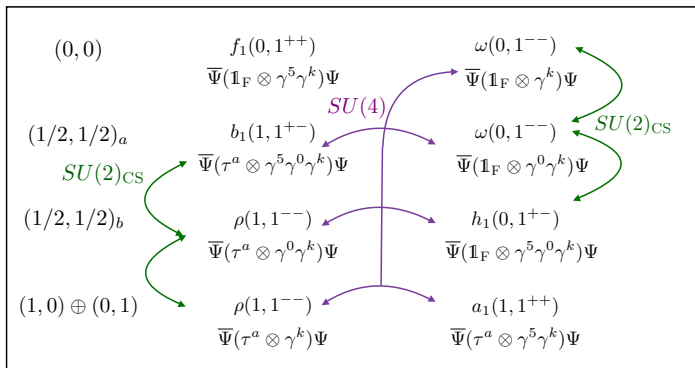
$$\psi = \begin{pmatrix} u_L \\ u_R \\ d_L \\ d_R \end{pmatrix}$$

and has the following set of generators:

$$\{(\tau^a \otimes \mathbb{1}_D), (\mathbb{1}_F \otimes \Sigma^i), (\tau^a \otimes \Sigma^i)\}$$

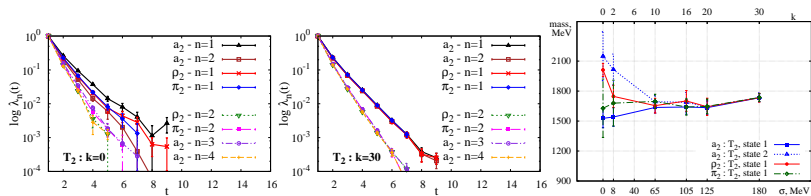
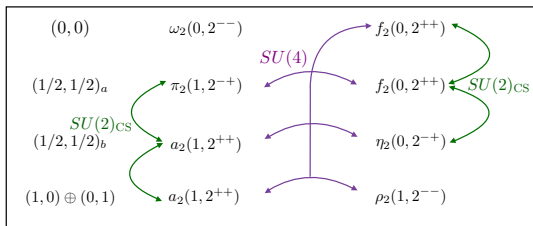


L.Ya.G., M. Pak, PRD 92(2015)016001

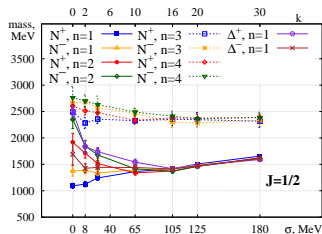
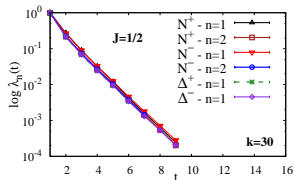
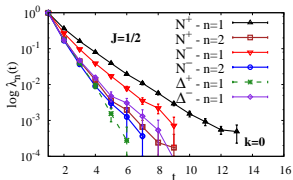


M. Denissenya, L.Ya.G, M.Pak, PRD 91(2015)114512

J=2 mesons.



$J = 1/2$ baryons: M. Denissenya, L.Ya.G, M.Pak, PRD 92 (2015) 074508



L.Ya.G., M. Pak, PRD 92(2015)016001

QCD Hamiltonian in Coulomb gauge (Christ and Lee):

$$H_{QCD} = H_E + H_B + \int d^3x \Psi^\dagger(\mathbf{x}) [-i\boldsymbol{\alpha} \cdot \boldsymbol{\nabla} + \beta m] \Psi(\mathbf{x}) + H_T + H_C,$$

$$H_T = -g \int d^3x \Psi^\dagger(\mathbf{x}) \boldsymbol{\alpha} \cdot \mathbf{A}(\mathbf{x}) \Psi(\mathbf{x}),$$

$$H_C = \frac{g^2}{2} \int d^3x d^3y J^{-1} \rho^a(\mathbf{x}) F^{ab}(\mathbf{x}, \mathbf{y}) J \rho^b(\mathbf{y}).$$

The Coulombic H_C part is a $SU(2)_{CS}$ - and $SU(4)$ - singlet. It is a confining part of the QCD Hamiltonian. This part generates a $SU(4)$ -symmetric spectrum.

The transverse (magnetic) part H_T is not $SU(2)_{CS}$ - and $SU(4)$ -symmetric and therefore its expectation value vanishes in the $SU(4)$ -symmetric hadron wave function.

The chromo-magnetic interaction contributes only to the near-zero modes while the confining chromo-electric interaction is distributed in all modes.



(Near) zero modes of Euclidean QCD and $SU(2)_{CS}$ - $SU(4)$ breaking.

The Euclidean $SU(2)_{CS}$ generators:

$$\Sigma = \{\gamma^k, -i\gamma^5\gamma^k, \gamma^5\}. \quad (1)$$

The $SU(2)_{CS}$ generators do not commute with the Dirac operator.

These symmetries are missing in the Lagrangian.

The intrinsic dynamical reason: the zero modes of the Dirac operator

$$\gamma_\mu D_\mu \Psi_0(x) = 0. \quad (2)$$

The zero mode is chiral, L or R , depending on the topological charge $Q \neq 0$.

Atiyah-Singer:

$$Q = n_L - n_R$$

At $Q \neq 0$, there is an asymmetry between L and R .

Conclusion: The zero modes break explicitly $SU(2)_{CS}$ and $SU(2N_F)$.



Conclusions to part I and prediction for high T

Observed on the lattice $SU(4)$ symmetry of hadrons upon elimination of the near-zero modes is a **symmetry of confinement in QCD** that is due to chromo-electric charge-charge interaction.

The **chromo-magnetic** interaction in QCD contributes only to near-zero modes. It breaks explicitly the $SU(4)$ symmetry of confinement.

The hadron spectra observed in real world can be viewed as a result of splitting of the primary energy levels with the $SU(4)$ symmetry by means of dynamics associated with the near-zero modes.

JLQCD: above T_c both $SU(2)_L \times SU(2)_R$ and $U(1)_A$ get restored and a gap opens in the spectrum of the Dirac operator. **Then we expect that the actual symmetry is $SU(4)$ - no deconfinement.**



Spacelike correlators at high T. Full QCD, no truncation.

C. Rohrhofer, Y. Aoki, G. Cossu, H. Fukaya, L.Ya.G., S. Hashimoto,
 C. B. Lang, S. Prelovsek, arXiv:1707.01881

$N_f = 2$ QCD with the chirally symmetric Dirac operator.

$$C_\Gamma(n_z) = \sum_{n_x, n_y, n_t} \langle \mathcal{O}_\Gamma(n_x, n_y, n_z, n_t) \mathcal{O}_\Gamma(\mathbf{0}, 0)^\dagger \rangle.$$

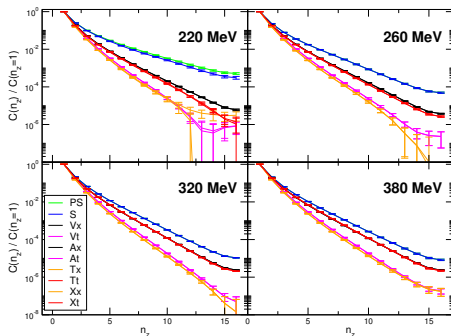
where $\mathcal{O}_\Gamma(x) = \bar{q}(x) \Gamma \frac{\mathbf{T}}{2} q(x)$ are all possible $J = 0$ and $J = 1$ local operators:

Name	Dirac structure	Abbreviation	
<i>Pseudoscalar</i>	γ_5	<i>PS</i>] $U(1)_A$
<i>Scalar</i>	$\mathbb{1}$	<i>S</i>	
<i>Axial-vector</i>	$\gamma_k \gamma_5$	A] $SU(2)_A$
<i>Vector</i>	γ_k	V	
<i>Tensor-vector</i>	$\gamma_k \gamma_3$	T] $U(1)_A$
<i>Axial-tensor-vector</i>	$\gamma_k \gamma_3 \gamma_5$	X	

Table : Operators considered in this work and their transformation properties. The open vector index k denotes the components 1, 2, 4, i.e. x, y, t .



Spatial correlators at high T. Full QCD, no truncation.



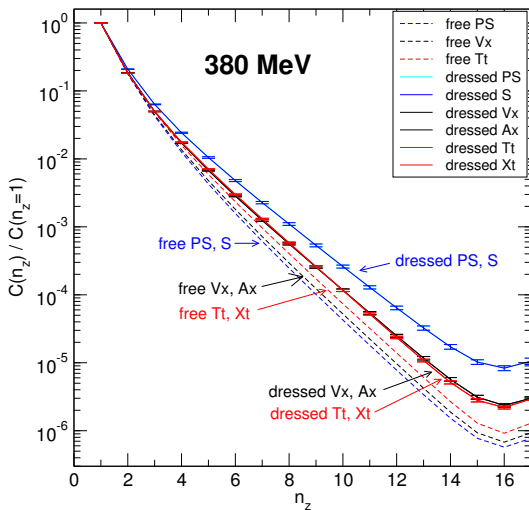
In total we observe three different multiplets:

$$E_1(U(1)_A) : \quad PS \leftrightarrow S$$

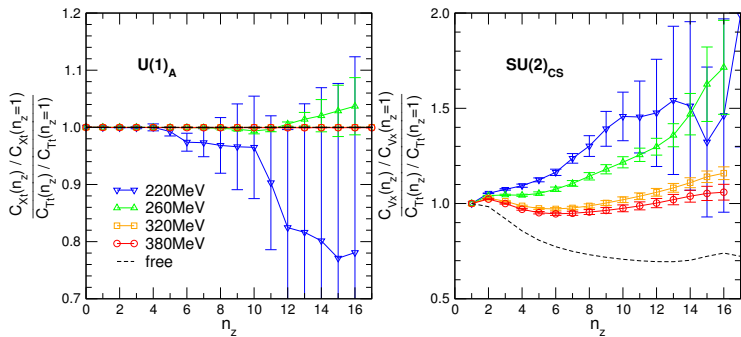
$$E_2(SU(4)) : \quad V_x \leftrightarrow T_t \leftrightarrow X_t \leftrightarrow A_x$$

$$E_3(SU(4)) : \quad V_t \leftrightarrow T_x \leftrightarrow X_x \leftrightarrow A_t$$

Spatial correlators at high T. Full QCD, no truncation.



Spatial correlators at high T. Full QCD, no truncation.



At $T=380$ MeV we observe approximate $SU(2)_{CS}$ and $SU(4)$ symmetries at the level of 5%.

Conclusions to part II

We observe emergence of approximate $SU(2)_{CS}$ and $SU(4)$ symmetries with increasing temperature.

It seems that we do not approach the free quark limit.

Emergence of $SU(2)_{CS}$ and $SU(4)$ symmetries indicates that the chromo-magnetic interaction is suppressed while confining chromo-electric interaction is still active.

These symmetries are incompatible with the scenario of a plasma of asymptotically free, deconfined quarks and gluons.

