

# $(g - 2)_\mu$ and scalar leptoquark(s)

**Olcyr Sumensari**

[hep-ph/1910.03877](https://arxiv.org/abs/hep-ph/1910.03877)

In collaboration with

**I. Doršner and S. Fajfer**

*Belica, October 10, 2019.*



**UNIVERSITÀ  
DEGLI STUDI  
DI PADOVA**

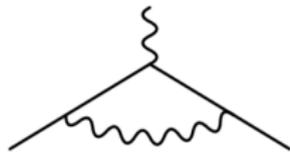
## Introduction

$(g - 2)_\mu$

Long-standing discrepancy [ $\approx 3.6 \sigma$ ] in  $(g - 2)_\mu$ :

$$a_\mu^{\text{exp}} = 116592089(63) \times 10^{-11}$$

$$a_\mu^{\text{SM}} = 116591820(36) \times 10^{-11}$$



[Brookhaven, 2006]

[Keshavarzi et al., '18], [Davier et al. '19]

⇒ Signal of **new bosons** coupled to **muons**?

⇒ **New results** by *Muon*  $g - 2$  at Fermilab will be **soon released!**

This talk: (i) **Brief overview**

(ii) **Single-leptoquark** solutions

(iii) Leptoquark mixing for  $(g - 2)_\mu$

# Brief overview

## Introduction: The anomalous magnetic moment

- Dirac equation predicts for a lepton  $\ell = e, \mu, \tau$ :

$$\vec{\mu}_\ell = g_\ell \frac{e}{2m_\ell} \vec{s}, \quad g_\ell = 2$$

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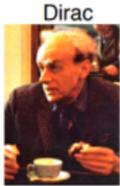
- Study the lepton-photon vertex:

$$\bar{u}(p')\Gamma_\mu u(p) = \bar{u}(p') \left[ \gamma_\mu \mathcal{F}_1(q^2) + \frac{i\sigma_{\mu\nu}q^\nu}{2m_\ell} \mathcal{F}_2(q^2) + \dots \right] u(p)$$

$$\mathcal{F}_1(0) = 1 \quad \mathcal{F}_2(0) = a_\ell \propto \frac{\alpha_{\text{em}}}{\pi} + \dots \approx 10^{-3}$$

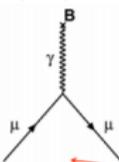
$\Rightarrow$  Pure quantum effect! Very sensitive probe of new physics

# Standard Model Components of muon g-2



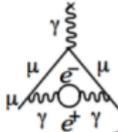
Dirac

Charged, spin 1/2 particle

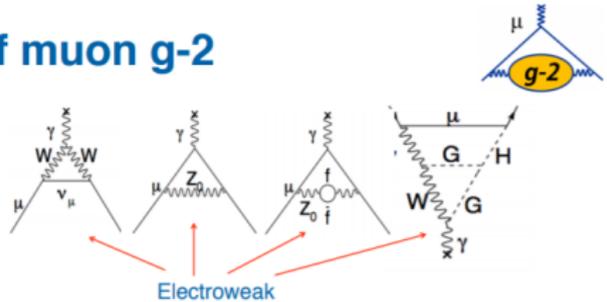


Kinosita

Up to 10<sup>th</sup> Order QED



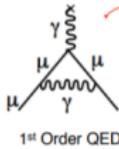
+12671 diagrams



$$g_\mu = 2.00233183636(86)$$

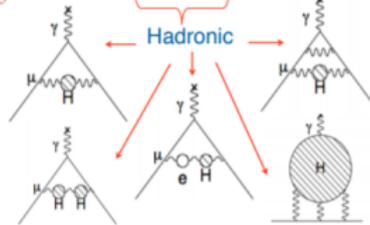


Schwinger



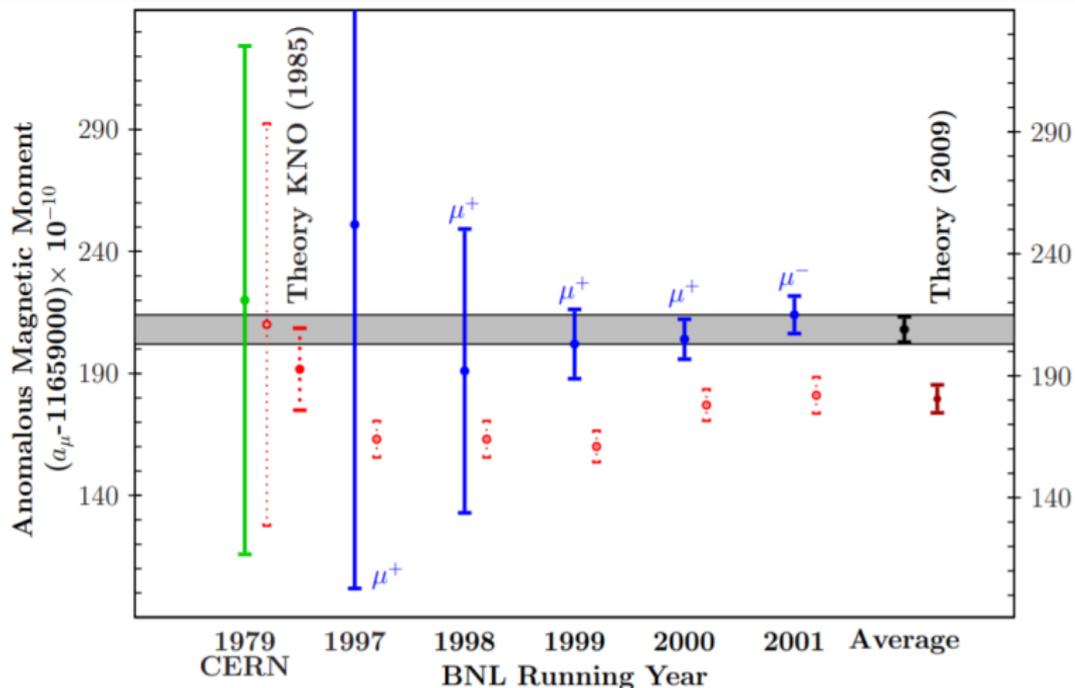
1<sup>st</sup> Order QED

$$\frac{\alpha}{2\pi} = 0.00232$$



SM uncertainty

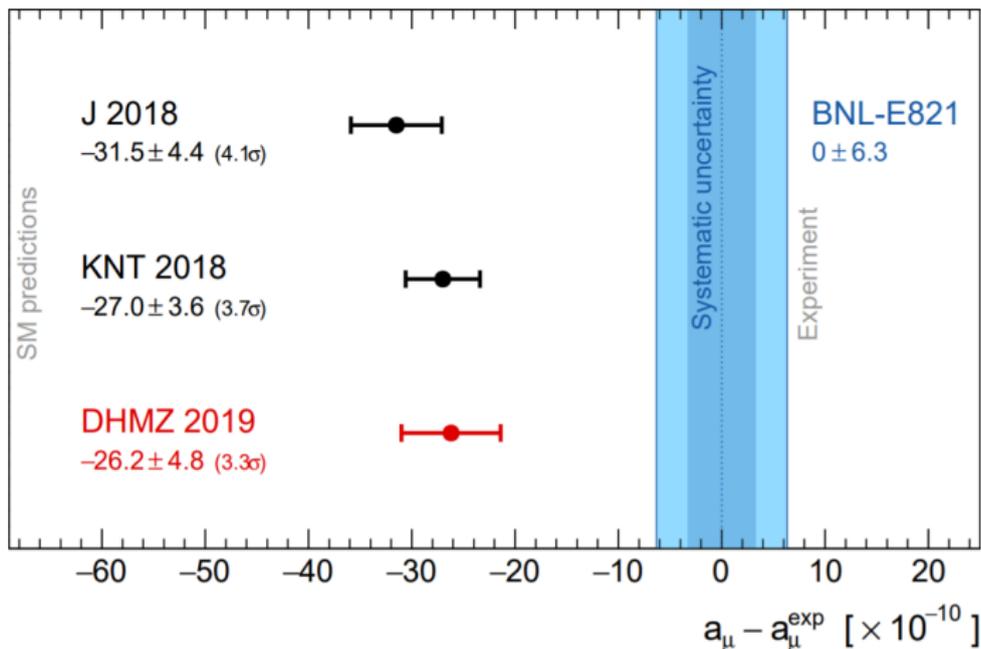
## History plot:



[Jegerlehner, Nyffeler. '09]

$\Rightarrow$  BNL delivered 0.5ppm precision.

## Current status

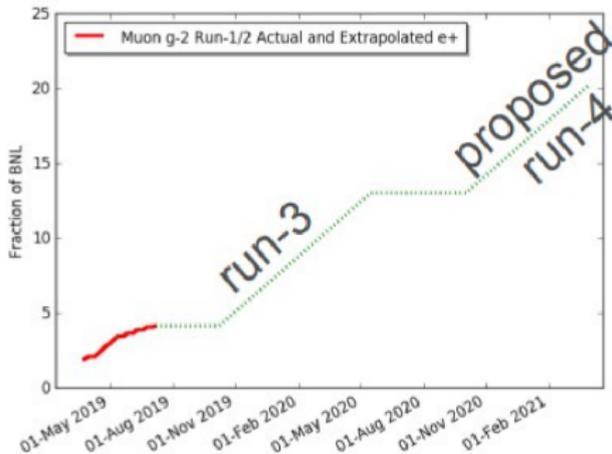
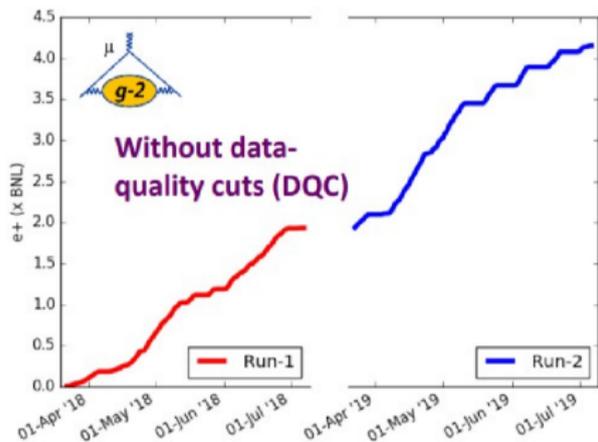


[Davier, Hoecker, Malaescu, Zhang.'19]

⇒ Fermilab aims to reduce the exp. error by  $\approx \times 4$ .

⇒ Effort to reduce the theory error, cf. "Muon ( $g - 2$ ) Th. Initiative".

Fermilab data collected compared to BNL:



[D. Hertzog talk at “Muon  $g - 2$  Th. Initiative Workshop”, '19]

⇒ News coming very soon!

# $(g - 2)_\mu$ and new physics: Leptoquarks

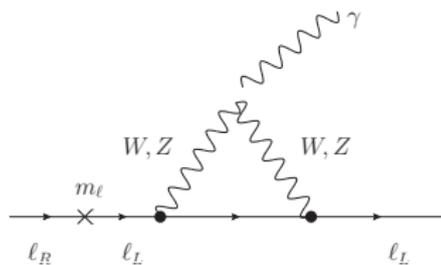
## $(g - 2)_\mu$ and new physics

- Current discrepancy is of similar size of SM electroweak loops:

Naive scaling:

$$\Delta a_\ell \propto \frac{m_\ell^2}{v^2}$$

[Giudice et al. '12]



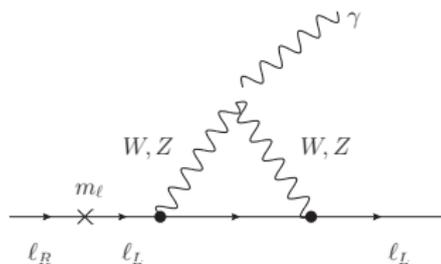
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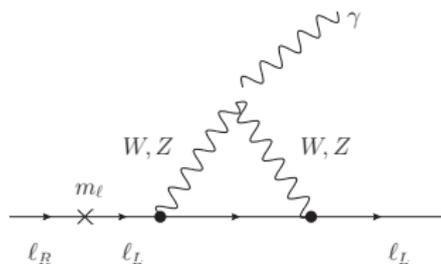
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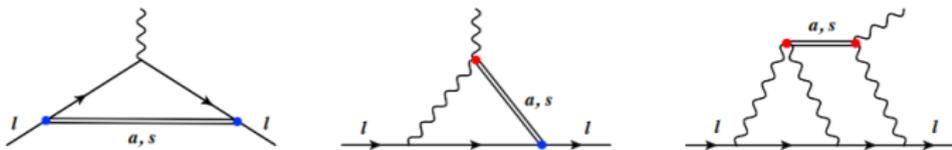
[Giudice et al. '12]



$\Rightarrow$  Either **new physics** is **light**, **and/or** an **enhancement** mechanism **takes place** (breaking the naive scaling).

- Popular solution: light (pseudo)scalar particles

[Marciano et al. '16]



see also [Bauer et al. '19], [Cornella, Paradisi, OS. In preparation]

## Leptoquarks and chiral enhancement

$$\begin{aligned}\Delta a_\mu &= a_\mu^{\text{exp}} - a_\mu^{\text{SM}} \\ &= (2.7 \pm 0.7) \times 10^{-9}\end{aligned}$$

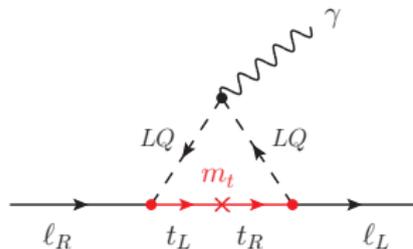
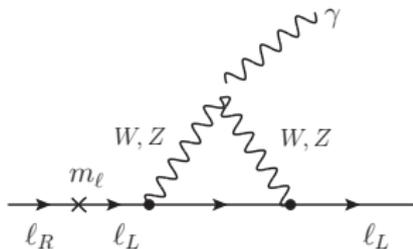
$$\mathcal{L} \supset \frac{c_{\text{dip}}}{\Lambda^2} \bar{L} \sigma_{\mu\nu} \ell_R H F^{\mu\nu} + \text{h.c.}$$

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- $\Delta a_\mu$  can be explained if  $\Delta a_\mu \propto \frac{m_\mu m_t}{\Lambda^2}$



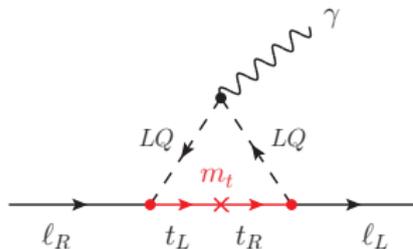
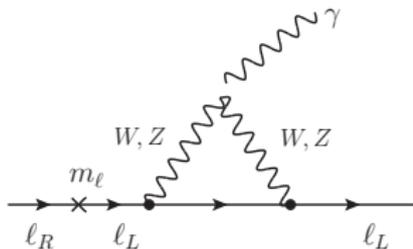
$\Rightarrow$  LQs should couple to  $\bar{\mu}_L t_R S$  and  $\bar{\mu}_R t_L S$ .

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⇒ LQs should couple to  $\bar{\mu}_L t_R S$  and  $\bar{\mu}_R t_L S$ .

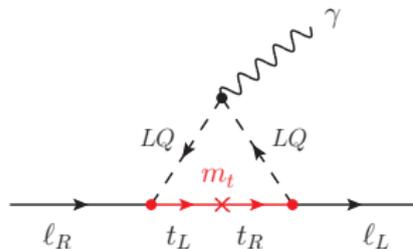
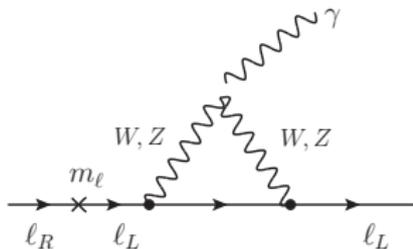
⇒ Perturbativity implies that  $m_{\text{LQ}} \lesssim 30 \text{ TeV}$ .

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$\Rightarrow$  LQs should couple to  $\bar{\mu}_L t_R S$  and  $\bar{\mu}_R t_L S$ .

$\Rightarrow$  Perturbativity implies that  $m_{LQ} \lesssim 30 \text{ TeV}$ .

$\Rightarrow$  Only two models are viable:  $S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$  and  $R_2 = (\mathbf{3}, \mathbf{2}, 7/6)$ .

[Cheung, '01]

## Leptoquarks for $(g - 2)_\mu$

Symbol	$(SU(3)_c, SU(2)_L, U(1)_Y)$	Interactions	$F = 3B + L$
$S_3$	$(\bar{\mathbf{3}}, \mathbf{3}, 1/3)$	$\bar{Q}^C L$	-2
$R_2$	$(\mathbf{3}, \mathbf{2}, 7/6)$	$\bar{u}_R L, \bar{Q} e_R$	0
$\tilde{R}_2$	$(\mathbf{3}, \mathbf{2}, 1/6)$	$\bar{d}_R L$	0
$\tilde{S}_1$	$(\bar{\mathbf{3}}, \mathbf{1}, 4/3)$	$\bar{d}_R^C e_R$	-2
$S_1$	$(\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	$\bar{Q}^C L, \bar{u}_R^C e_R$	-2

- Are there other potentially large contributions in LQ models?
- What if more than one scalar LQ exist?

## Leptoquark mixing for $(g - 2)_\mu$

[Dorsner, Fajfer, **OS**. 1910.03877].

## Why two scalar LQs?

⇒ Having more than one LQ is **motivated** by **theory/phenomenology**:

- $SU(5)$  unification possible with two light scalar LQs.  
cf. e.g. [Dorsner et. al. '18]
- Models for radiative **neutrino masses**.  
[Mahanta, '99], [Chua et al. '99]
- $B$ -physics anomalies require more than one (scalar) LQ.  
[Angelescu, Becirevic, Faroughy, OS. '18]

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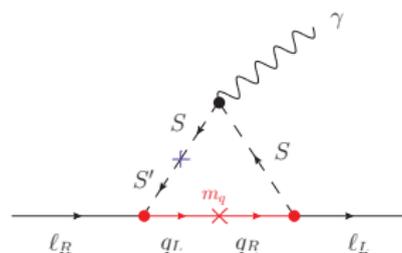
[Angelescu, Becirevic, Faroughy, OS. '18]

## Leptoquark mixing

⇒ Scalar LQs can **mix** with the **SM Higgs** (cf. [Hirsch. '06]), inducing **new contributions** to dipoles!

[Dorsner, Fajfer, OS. 1910.03877].

$$\mathcal{L} \supset \xi HHSS' \quad \text{or} \quad g HSS'$$



⇒ **Chirality enhancement** induced by **mixing** of chiral LQs!

LQ pairs	Mixing field(s)	$(g-2)_\mu$	$\nu$ -mass
$S_1 - S_3$	$H H$	$u$	–
$\tilde{S}_1 - S_3$	$H H$	$d$	–
$\tilde{R}_2 - R_2$	$H H$	$d$	–
$\tilde{R}_2 - S_1$	$H$	–	$d$
$\tilde{R}_2 - S_3$	$H$	–	$d$

- Two new possibilities with non-chiral LQs – but stemming from different couplings:  $R_2 - \tilde{R}_2$  and  $S_1 - S_3$ .
- One entirely new scenario:  $\tilde{S}_1 - S_3$ .

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Remainder of this talk: (i) How does it work?  $S_1 - S_3$  via top loops  
(iii) Mixing scenarios with  $b$ -quark loops

## How does it work?

Example:  $S_1$ - $S_3$  via top loops

## How does it work?

- Take two scalars  $S_a^{(Q)}$  and  $S_b^{(Q)}$ , from different EW multiplets, with same electric charge  $Q$ , and mass matrix:

$$\mathcal{M}^2 = \begin{pmatrix} m_{S_a}^2 & \Omega \\ \Omega & m_{S_b}^2 \end{pmatrix}$$

where  $\Omega$  is the **mixing term** and  $m_{S_{a,b}}$  are the **masses prior to mixing**.

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- **New mass eigenstates** with charge  $Q$  are:

$$\begin{pmatrix} S_+^{(Q)} \\ S_-^{(Q)} \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} S_a^{(Q)} \\ S_b^{(Q)} \end{pmatrix}, \quad \tan 2\theta = \frac{2\Omega}{m_{S_a}^2 - m_{S_b}^2}$$

with

$$m_{S_{\pm}^{(Q)}}^2 = \frac{m_{S_a}^2 + m_{S_b}^2}{2} \pm \frac{1}{2} \sqrt{(m_{S_a}^2 - m_{S_b}^2)^2 + 4\Omega^2},$$

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- Maximal mixing ( $\theta = \pi/4$ ) can arise for  $m_S \equiv m_{S_a} = m_{S_b}$ :

$$\delta m_S^{(Q)} \equiv m_{S_+}^{(Q)} - m_S \simeq m_S - m_{S_-}^{(Q)} \quad (m_{S_{a,b}} \gg \Omega)$$

Example:  $S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$  &  $S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$

$(g - 2)_\mu$

$$\mathcal{L}_{S_1} = y_R^{ij} \overline{u_{Ri}^C} e_{Rj} S_1 + \text{h.c.},$$

$$\mathcal{L}_{S_3} = y_L^{ij} \overline{Q_i^C} i\tau_2(\vec{\tau} \cdot \vec{S}_3)L_j + \text{h.c.},$$

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These states can **mix** via the **SM Higgs**:

$$\mathcal{L}_{\text{mix}} \supset \xi H^\dagger (\vec{\tau} \cdot \vec{S}_3) H S_1^* + \text{h.c.} \quad \Rightarrow \quad \mathcal{M}_{S(1/3)}^2 = \begin{pmatrix} m_{S_3}^2 & -\frac{\xi v^2}{2} \\ -\frac{\xi v^2}{2} & m_{S_1}^2 \end{pmatrix}$$

Mass eigenstates:

$$\begin{pmatrix} S_+^{(1/3)} \\ S_-^{(1/3)} \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} S_3^{(1/3)} \\ S_1^{(1/3)} \end{pmatrix}.$$

$\Rightarrow$  Both mass-eigenstates have couplings with  $\overline{u_L^C} e_L$  and  $\overline{u_R^C} e_R$ .

Example:  $S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$  &  $S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$

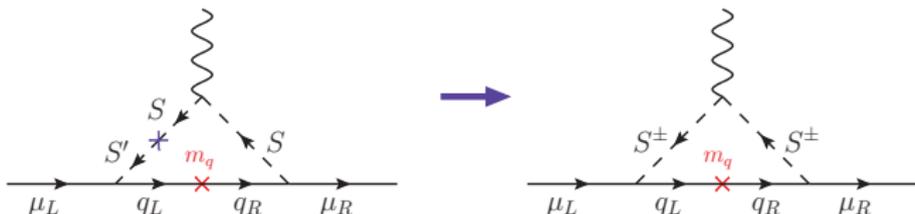
$(g-2)_\mu$

Yukawa choice:

$$\mathcal{L}_{S_1} = y_R^{ij} \overline{u_{Ri}^C} e_{Rj} S_1 + \text{h.c.},$$

$$\mathcal{L}_{S_3} = y_L^{ij} \overline{Q_i^C} i\tau_2 (\vec{\tau} \cdot \vec{S}_3) L_j + \text{h.c.},$$

with  $y_{t\mu}^L \neq 0$  and  $y_{t\mu}^R \neq 0$ .

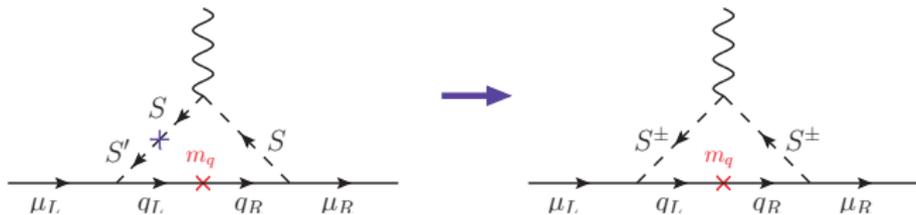


Four mass-eigenstates:  $m_S \equiv m_{S_3}^{(4/3)} = m_{S_3}^{(2/3)}$  and  $m_{S_\pm} \equiv m_{S_\pm}^{(1/3)}$ .

Example:  $S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$  &  $S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$

$(g-2)_\mu$

• **Chirality-enhanced** contribution:



$$\delta a_\mu \propto \frac{m_\mu^2}{m_S^2} (\dots) + m_\mu m_t y_L^{b\mu} y_R^{t\mu*} \left[ \frac{\mathcal{G}_{1/3}(x_t^+)}{m_{S^+}^2} - \frac{\mathcal{G}_{1/3}(x_t^-)}{m_{S^-}^2} \right]$$

with  $x_t^\pm = m_t^2/m_{S^\pm}^2$ .

• For **maximal mixing** ( $\theta = \pi/4$ ), this contribution reads

$$\delta a_\mu \propto \frac{m_\mu m_t}{m_S^2} \frac{\delta m_S}{m_S} y_R^{b\mu} y_L^{t\mu}$$

$\Rightarrow$  **Crucial:** How do we fix  $\delta m_S$ ?

Example:  $S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$  &  $S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$

EWPT

$T$ -parameter:

$$\Delta T = -\frac{N_c}{4\pi c_w^2 s_w^2} \frac{1}{m_Z^2} \left[ \cos^2 \theta F(m_{S_3}, m_{S_-}) + \sin^2 \theta F(m_{S_3}, m_{S_+}) \right],$$

with  $F(m, m) = 0$ .



Example:  $S_1 = (\bar{3}, 1, 1/3)$  &  $S_3 = (\bar{3}, 3, 1/3)$

EWPT

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Expanding on  $\delta m_S$  for maximal mixing ( $\theta = \pi/4$ ):

$$\Delta T = \frac{N_c}{3\pi c_w^2 s_w^2} \frac{\delta m_S^2}{m_Z^2} + \dots$$

$$\Delta T^{\text{exp}} = 0.05(12)$$

$\Rightarrow$

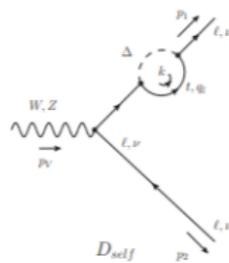
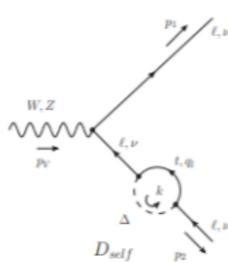
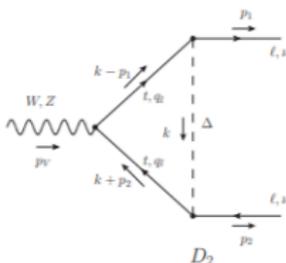
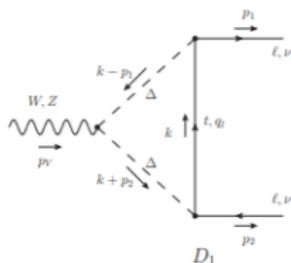
$$|\delta m_S| \lesssim 40 \text{ GeV}$$

[Gfitter. '12]

LQs modify the  $Z$ -couplings to leptons at one-loop:

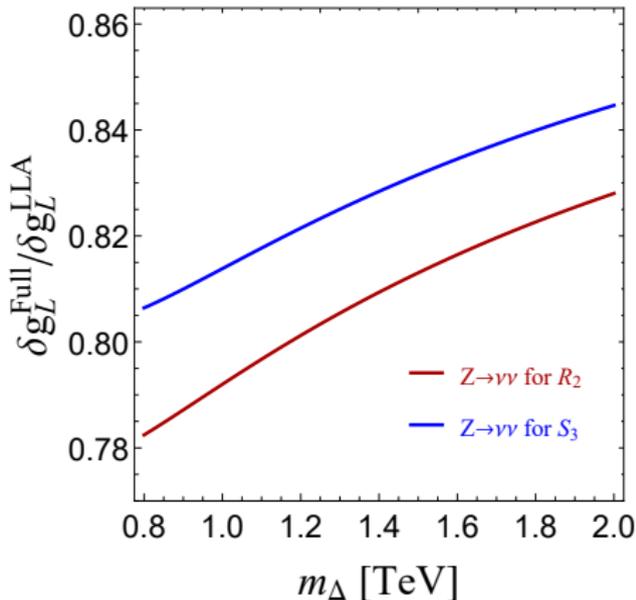
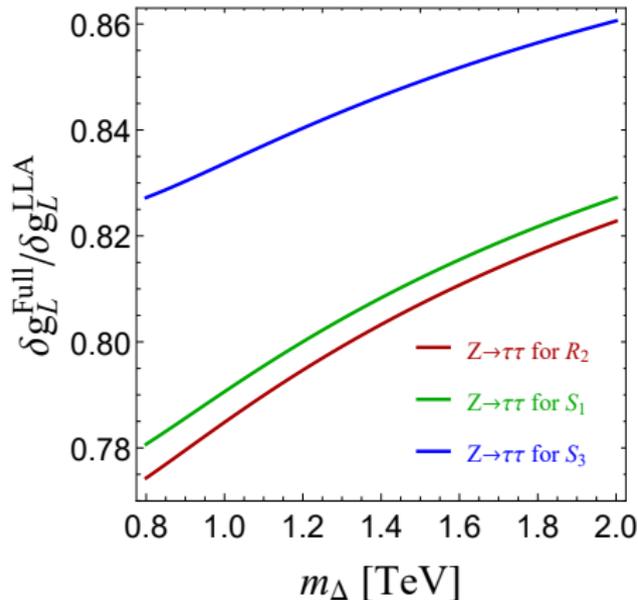
$$\delta\mathcal{L}_{\text{eff}}^Z = \frac{g}{\cos\theta_W} \sum_{i,j} \bar{\ell}_i \gamma^\mu \left[ g_{\ell_L}^{ij} P_L + g_{\ell_R}^{ij} P_R \right] \ell_j Z_\mu$$

$$g_{\ell_{L(R)}}^{ij} = \delta_{ij} g_{\ell_{L(R)}}^{\text{SM}} + \delta g_{\ell_{L(R)}}^{ij}$$



⇒ Complete one-loop computation: [Arnan, Becirevic, Mescia, OS. '19]

[Arnan, Becirevic, Mescia, OS. '19]



$\Rightarrow$  To compare with leading-log approximation (LLA). cf. [Feruglio et al. '16]

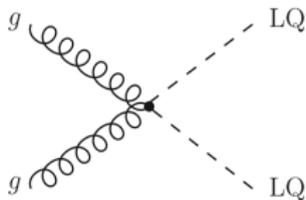
$\Rightarrow$   $\mathcal{O}(20\%)$  corrections due to external momenta ( $\propto x_Z \log x_t$ ) not considered before. cf. e.g. [Neubert et al. '15], [Buttazo et al. '17] + many more

## LHC constraints

$$U_1 = (3, 1, 2/3)$$

- LQ pair-production via QCD:

[CMS-PAS-EXO-17-003]

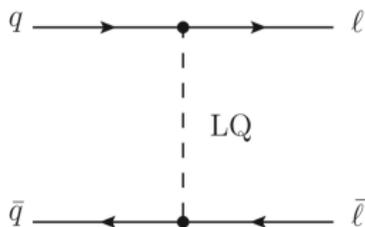


$$m_S \gtrsim 1.6 \text{ TeV}$$

[conservative choice;  $q\mu$  final state]

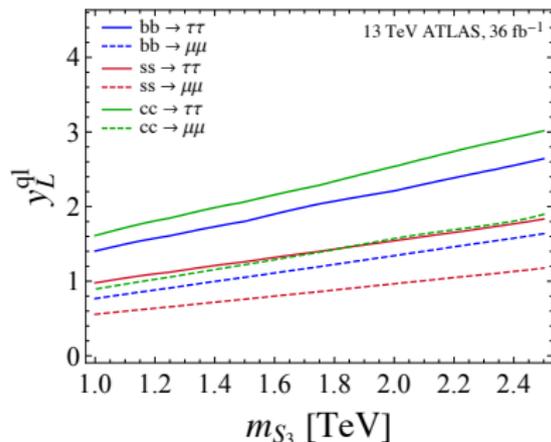
- Di-lepton tails at high-pT:

[ATLAS. 1707.02424,1709.07242]



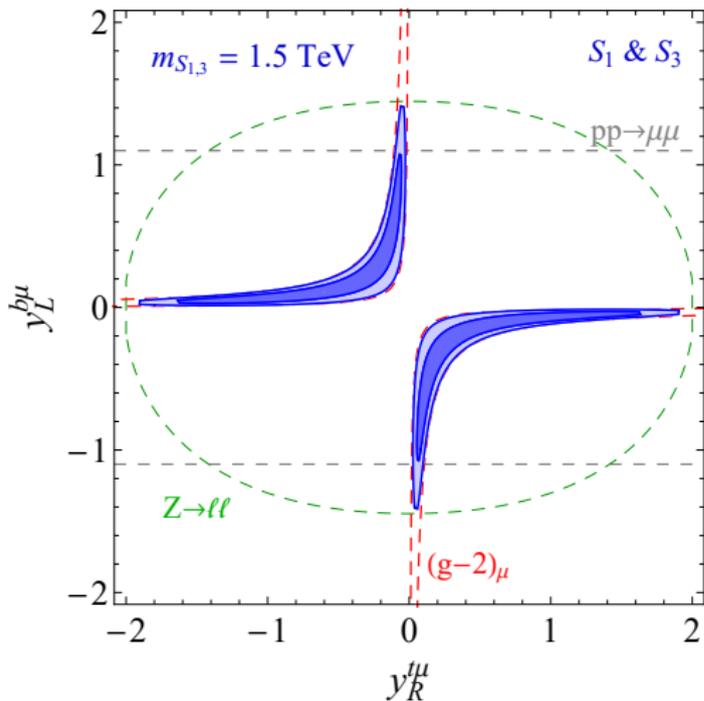
[Angelescu, Becirevic, Faroughy, OS. '18]

[see also Faroughy et al. '15]



## Combining everything

$$S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3) \text{ \& } S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$$

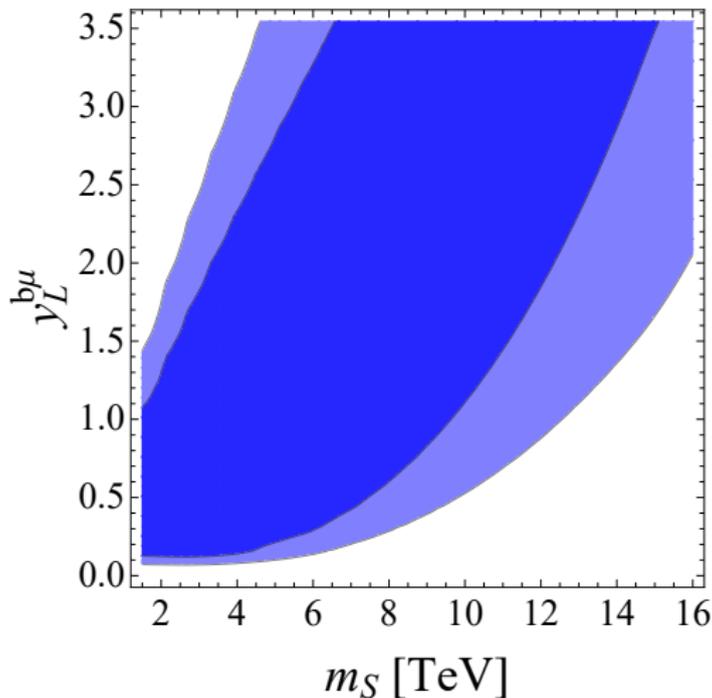


Benchmark:

- Maximal mixing ( $\theta = \pi/4$ ).
- $\delta m_S = 40 \text{ GeV}$  (EWPT).

How heavy can the LQs be?

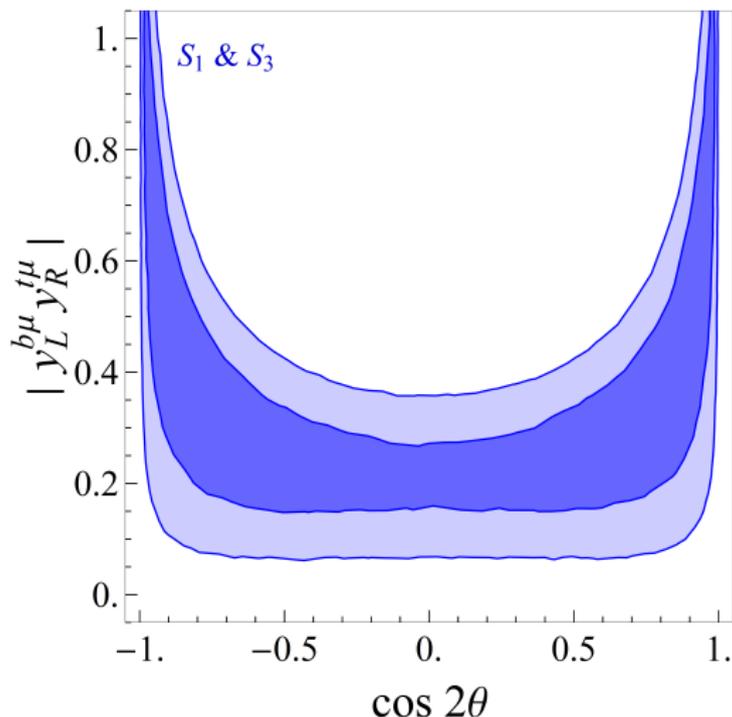
$S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$  &  $S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$



$\Rightarrow$  Yukawa perturbativity ( $\lesssim \sqrt{4\pi}$ )  $\Rightarrow m_S \lesssim 15$  TeV.

## Maximal mixing or not?

$$S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3) \text{ \& } S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$$



⇒ It does not change much...

## Other possibilities: $b$ -quark loops

Reminder:

Symbol	$(SU(3)_c, SU(2)_L, U(1)_Y)$	Interactions	$F = 3B + L$
$S_3$	$(\bar{\mathbf{3}}, \mathbf{3}, 1/3)$	$\bar{Q}^C L$	-2
$R_2$	$(\mathbf{3}, \mathbf{2}, 7/6)$	$\bar{u}_R L, \bar{Q} e_R$	0
$\tilde{R}_2$	$(\mathbf{3}, \mathbf{2}, 1/6)$	$\bar{d}_R L$	0
$\tilde{S}_1$	$(\bar{\mathbf{3}}, \mathbf{1}, 4/3)$	$\bar{d}_R^C e_R$	-2
$S_1$	$(\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	$\bar{Q}^C L, \bar{u}_R^C e_R$	-2

- Yukawa choice:

$$\mathcal{L}_{\tilde{R}_2} = -y_L^{ij} \bar{d}_{Ri} \tilde{R}_2 i\tau_2 L_j + \text{h.c.},$$

$$\mathcal{L}_{R_2} = y_R^{ij} \bar{Q}_i e_{Rj} R_2 + \text{h.c.}.$$

with  $y_{b\mu}^L \neq 0$  and  $y_{b\mu}^R \neq 0$ .

- Yukawa choice:

$$\mathcal{L}_{\tilde{R}_2} = -y_L^{ij} \bar{d}_{Ri} \tilde{R}_2 i\tau_2 L_j + \text{h.c.},$$

$$\mathcal{L}_{R_2} = y_R^{ij} \bar{Q}_i e_{Rj} R_2 + \text{h.c.}.$$

with  $y_{b\mu}^L \neq 0$  and  $y_{b\mu}^R \neq 0$ .

- Mixing with SM Higgs:

see also [Kosnik. '12]

$$\mathcal{L}_{\text{mix}}^{\tilde{R}_2 \& R_2} = -\xi (R_2^\dagger H) (\tilde{R}_2^T i\tau_2 H) + \text{h.c.}.$$

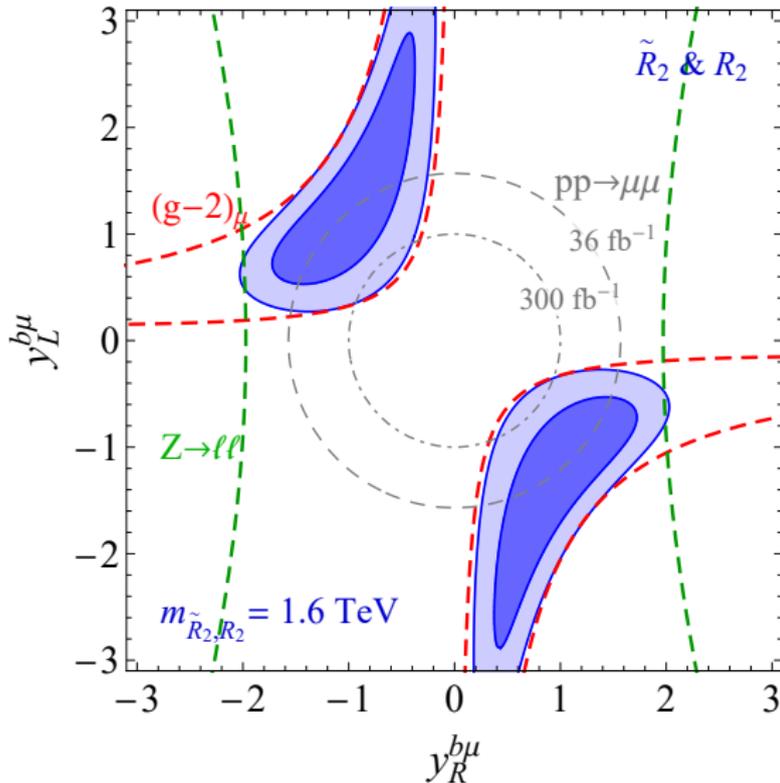
$\Rightarrow$  Mixing of  $Q = 2/3$  components of doublets.

$\Rightarrow$  EWPT gives  $\delta m_S \lesssim 50 \text{ GeV}$  for maximal mixing.

$\Rightarrow$  **Diquark couplings forbidden by gauge invariance.**

# Other possibilities - I

$$R_2 = (\mathbf{3}, \mathbf{2}, 7/6) \quad \& \quad \tilde{R}_2 = (\mathbf{3}, \mathbf{2}, 1/6)$$



- Yukawa choice:

$$\mathcal{L}_{\tilde{S}_1} = y_R^{ij} \bar{d}_{Ri}^C e_{Rj} \tilde{S}_1 + \text{h.c.},$$

$$\mathcal{L}_{S_3} = y_L^{ij} \bar{Q}_i^C i\tau_2(\vec{\tau} \cdot \vec{S}_3)L_j + \text{h.c.},$$

with  $y_{b\mu}^L \neq 0$  and  $y_{b\mu}^R \neq 0$ .

- Yukawa choice:

$$\mathcal{L}_{\tilde{S}_1} = y_R^{ij} \bar{d}_{Ri}^C e_{Rj} \tilde{S}_1 + \text{h.c.},$$

$$\mathcal{L}_{S_3} = y_L^{ij} \bar{Q}_i^C i\tau_2(\vec{\tau} \cdot \vec{S}_3)L_j + \text{h.c.},$$

with  $y_{b\mu}^L \neq 0$  and  $y_{b\mu}^R \neq 0$ .

- Mixing with SM Higgs:

$$\mathcal{L}_{\text{mix}}^{\tilde{S}_1 \& S_3} = \xi H^T i\tau_2(\vec{\tau} \cdot \vec{S}_3)H\tilde{S}_1^* + \text{h.c.},$$

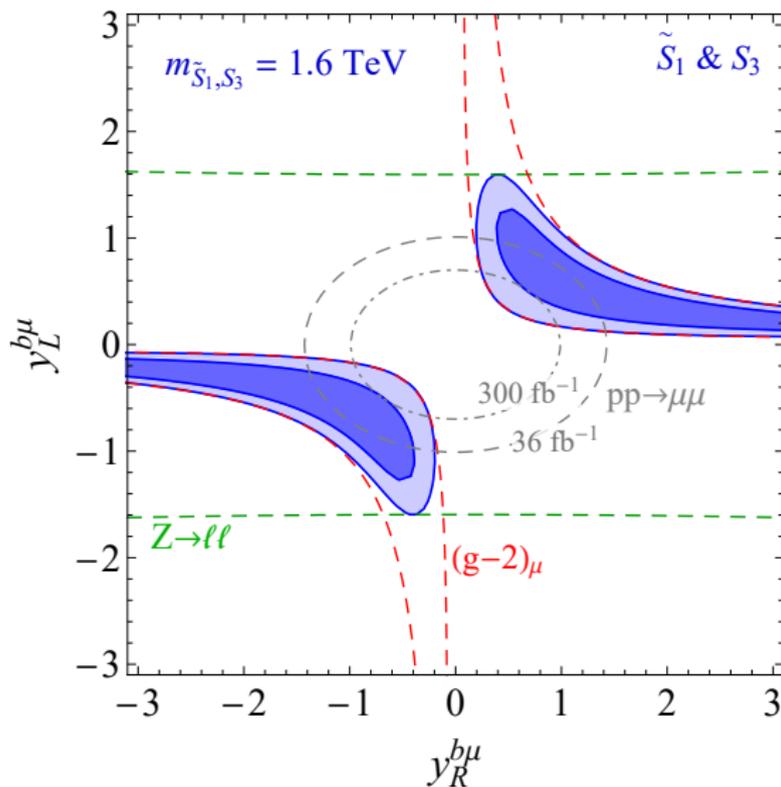
⇒ Mixing of  $Q = 4/3$  components of doublets.

⇒ EWPT gives  $\delta m_S \lesssim 50 \text{ GeV}$  for maximal mixing.

⇒ **Entirely new scenario!**

# Other possibilities - II

$$\tilde{S}_1 = (\bar{\mathbf{3}}, \mathbf{1}, 4/3) \text{ \& } S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$$



## Summary and perspectives

- $(g - 2)_\mu$  remains one of the most precise tests of the SM validity.  
Clarification from Fermilab coming soon!
- We summarize the viable single LQ explanations to  $(g - 2)_\mu$ .  
Top-quark chirality enhancement  $\Rightarrow m_S \lesssim 30$  TeV
- We propose the mixing of two scalar LQs as a new mechanism for chirality enhancement and identify three new viable scenarios  
Complementarity between EWPT, LHC and flavor data
- Building a concrete model to simultaneously explain  $(g - 2)_\mu$  and the  $B$ -physics anomalies remains a very challenging task.  
Data-driven model building!

**Thank you!**

# Back-up

# Limits on LQ pair-production

[Angelescu, Becirevic, Faroughy, OS. 1808.08179]

Decays	LQs	Scalar LQ limits	Vector LQ limits	$\mathcal{L}_{\text{int}}$ / Ref.
$jj \tau \bar{\tau}$	$S_1, R_2, S_3, U_1, U_3$	–	–	–
$b\bar{b} \tau \bar{\tau}$	$R_2, S_3, U_1, U_3$	850 (550) GeV	1550 (1290) GeV	12.9 fb <sup>-1</sup> [49]
$t\bar{t} \tau \bar{\tau}$	$S_1, R_2, S_3, U_3$	900 (560) GeV	1440 (1220) GeV	35.9 fb <sup>-1</sup> [50]
$jj \mu \bar{\mu}$	$S_1, R_2, S_3, U_1, U_3$	1530 (1275) GeV	2110 (1860) GeV	35.9 fb <sup>-1</sup> [51]
$b\bar{b} \mu \bar{\mu}$	$R_2, U_1, U_3$	1400 (1160) GeV	1900 (1700) GeV	36.1 fb <sup>-1</sup> [52]
$t\bar{t} \mu \bar{\mu}$	$S_1, R_2, S_3, U_3$	1420 (950) GeV	1780 (1560) GeV	36.1 fb <sup>-1</sup> [53, 54]
$jj \nu \bar{\nu}$	$R_2, S_3, U_1, U_3$	980 (640) GeV	1790 (1500) GeV	35.9 fb <sup>-1</sup> [55]
$b\bar{b} \nu \bar{\nu}$	$S_1, R_2, S_3, U_3$	1100 (800) GeV	1810 (1540) GeV	35.9 fb <sup>-1</sup> [55]
$t\bar{t} \nu \bar{\nu}$	$R_2, S_3, U_1, U_3$	1020 (820) GeV	1780 (1530) GeV	35.9 fb <sup>-1</sup> [55]

## $B$ -anomalies

Model	$R_{D^{(*)}}$	$R_{K^{(*)}}$	$R_{D^{(*)}}$ & $R_{K^{(*)}}$
$S_1 = (\bar{3}, 1, 1/3)$	✓	✗*	✗
$R_2 = (3, 2, 7/6)$	✓	✗*	✗
$S_3 = (\bar{3}, 3, 1/3)$	✗	✓	✗
$U_1 = (3, 1, 2/3)$	✓	✓	✓
$U_3 = (3, 3, 2/3)$	✗	✓	✗

[Angelescu, Becirevic, Faroughy, OS. '18]

$$\begin{aligned}
\delta a_\mu = & -\frac{N_c m_\mu^2}{8\pi^2} \left\{ 2 |y_L^{b\mu}|^2 \frac{\mathcal{F}_{4/3}(x_b)}{m_{S_3}^2} + \left[ \sin^2 \theta |y_R^{t\mu}|^2 + \cos^2 \theta |y_L^{b\mu}|^2 \right] \frac{\mathcal{F}_{1/3}(x_t^-)}{m_{S_-}^2} \right. \\
& + \left[ \cos^2 \theta |y_R^{t\mu}|^2 + \sin^2 \theta |y_L^{b\mu}|^2 \right] \frac{\mathcal{F}_{1/3}(x_t^+)}{m_{S_+}^2} \\
& \left. + \frac{m_t}{m_\mu} \sin \theta \cos \theta \operatorname{Re}(y_L^{b\mu} y_R^{t\mu*}) \left[ \frac{\mathcal{G}_{1/3}(x_t^+)}{m_{S_+}^2} - \frac{\mathcal{G}_{1/3}(x_t^-)}{m_{S_-}^2} \right] \right\},
\end{aligned}$$